



# Software für Statik und Dynamik

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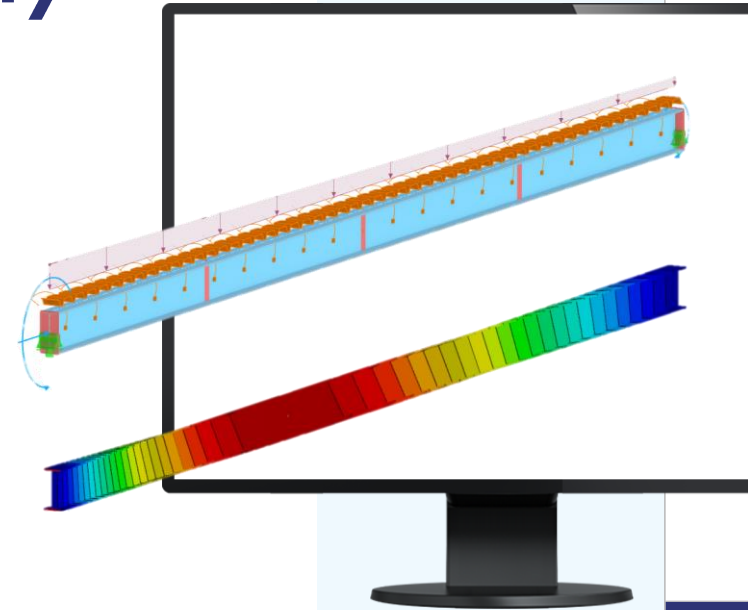


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Webinar

# Linear Stability Analysis in RFEM 6 and RSTAB 9



# Questions During the Presentation



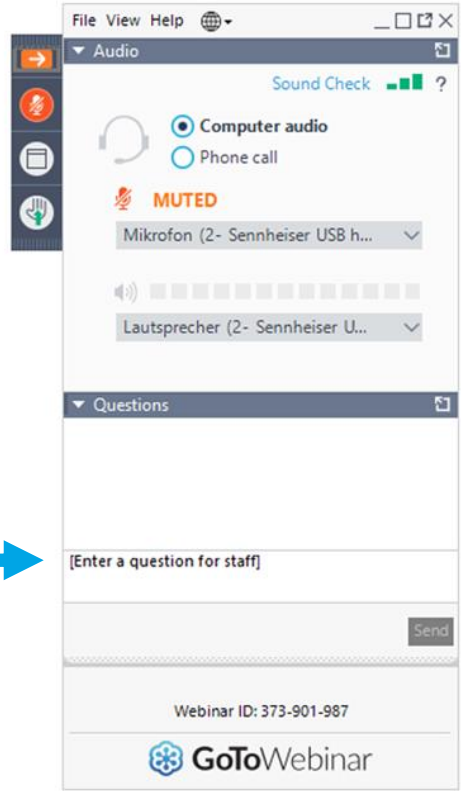
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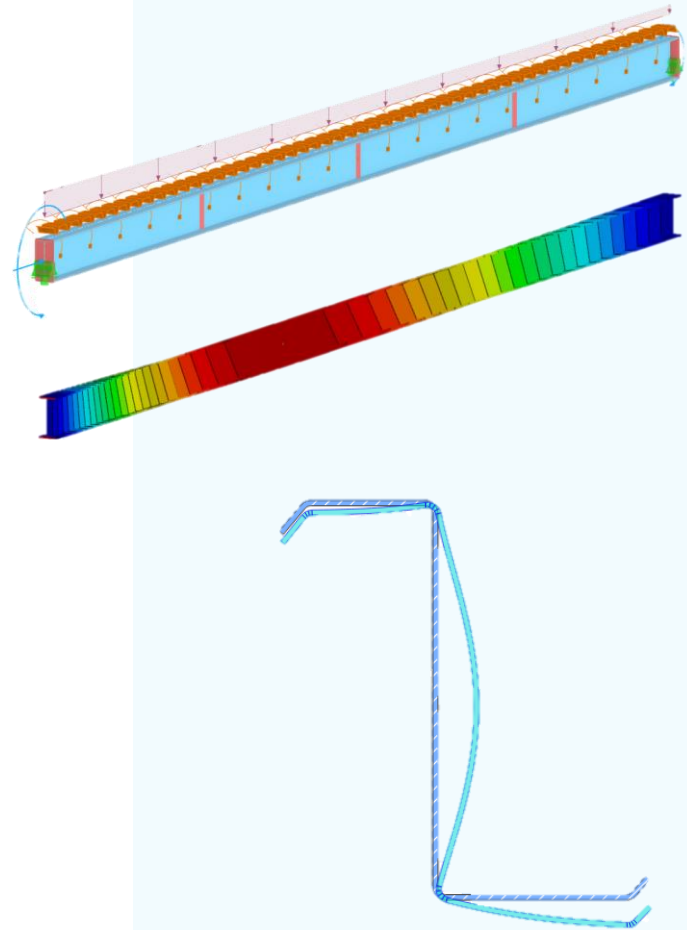
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Ask questions



# Content

- 01 **Stability analysis of members and frame structures**
- 02 **Stability analysis on cross section level using the finite strip method**
- 03 **Buckling analysis within steel joints**
- 04 **Detecting modeling errors and instability troubleshooting using stability analysis**





# Stability analysis as an eigenvalue problem

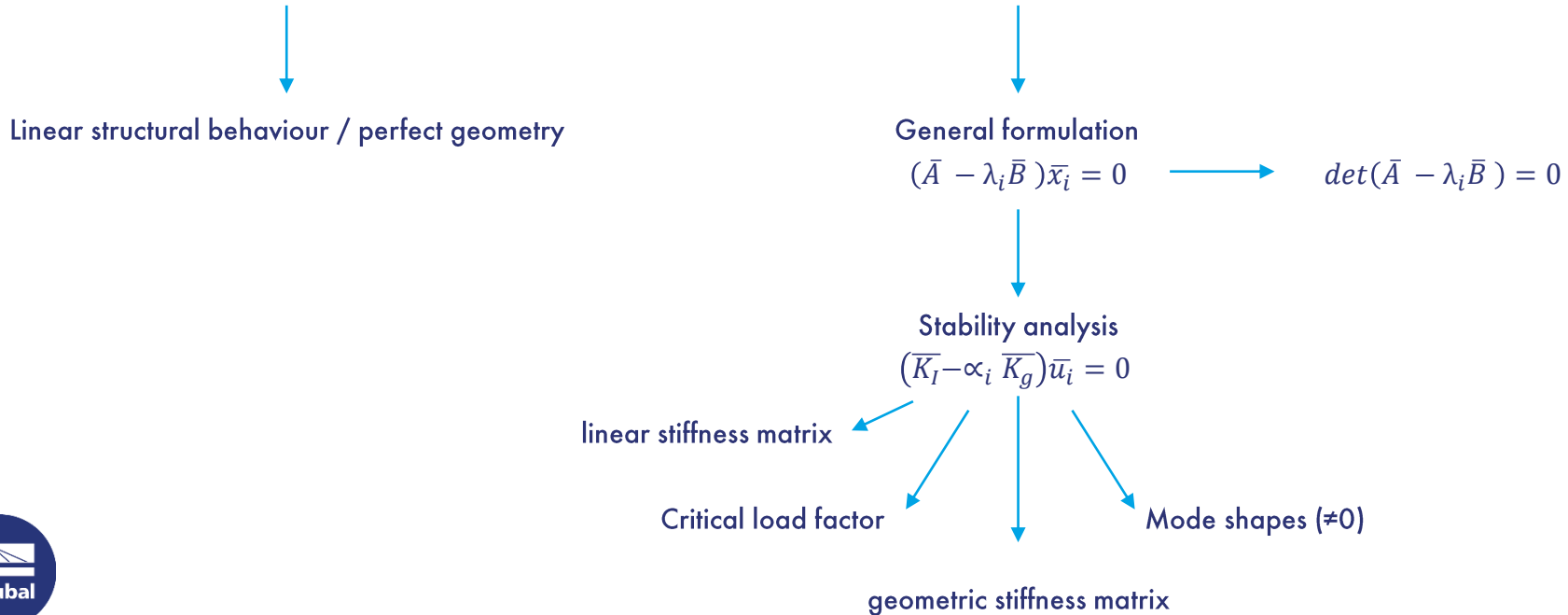
- **Slender** members and structures under compression tend to become **unstable**





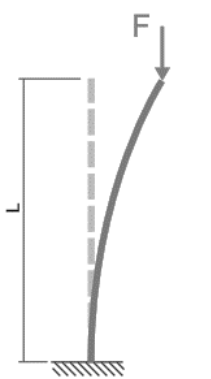
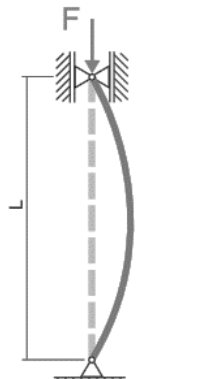
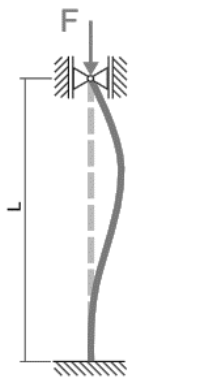
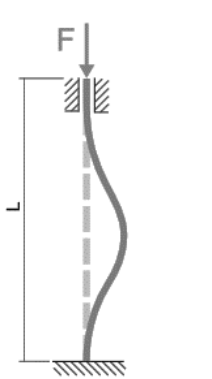
# Stability analysis as an eigenvalue problem

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- Using FEM, the **ideal** bifurcation load can be determined solving a conventional **Eigenvalue problem**



# Stability analysis as an eigenvalue problem

- **Slender** members and structures under compression tend to become **unstable**
- Using FEM, the **ideal** bifurcation load can be determined solving a conventional **Eigenvalue problem**
- Fundamental solutions for prismatic members under pure compression were already found by **Euler** in the 18<sup>th</sup> century.

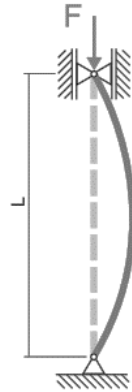
			
<b>Case 1</b>	<b>Case 2</b>	<b>Case 3</b>	<b>Case 4</b>
$F_{crit} = \frac{\pi^2 EI}{(2.0L)^2}$	$F_{crit} = \frac{\pi^2 EI}{(1.0L)^2}$	$F_{crit} = \frac{\pi^2 EI}{(0.7L)^2}$	$F_{crit} = \frac{\pi^2 EI}{(0.5L)^2}$

\*Buckling length coefficient



# Stability analysis as an eigenvalue problem

- **Slender** members and structures under compression tend to become **unstable**
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Case 2

$$F_{crit} = \frac{\pi^2 EI}{(1.0L)^2}$$

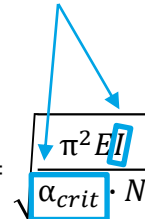


$$\beta L = L_{crit} = \sqrt{\frac{\pi^2 EI}{F_{crit}}}$$



$$L_{crit} = \sqrt{\frac{\pi^2 EI}{\alpha_{crit} \cdot N}}$$

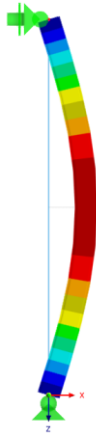
Mode shape dependent!





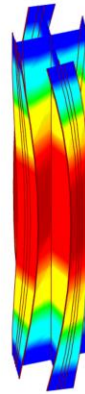


# Stability modes of beams



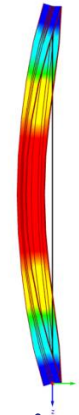
**Flexural buckling**

$$N_{cr,y/z}$$



**Torsional buckling**

$$N_{cr,T}$$

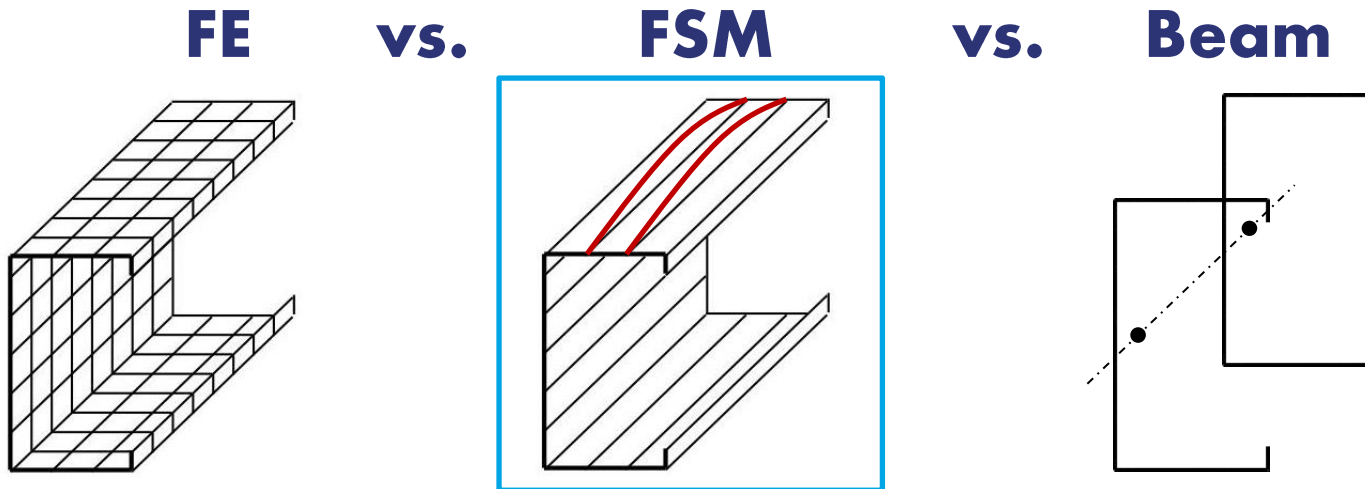


**Flexural-torsional Buckling**

**Lateral-torsional Buckling**

$$N_{cr,LTB} ; M_{cr}$$

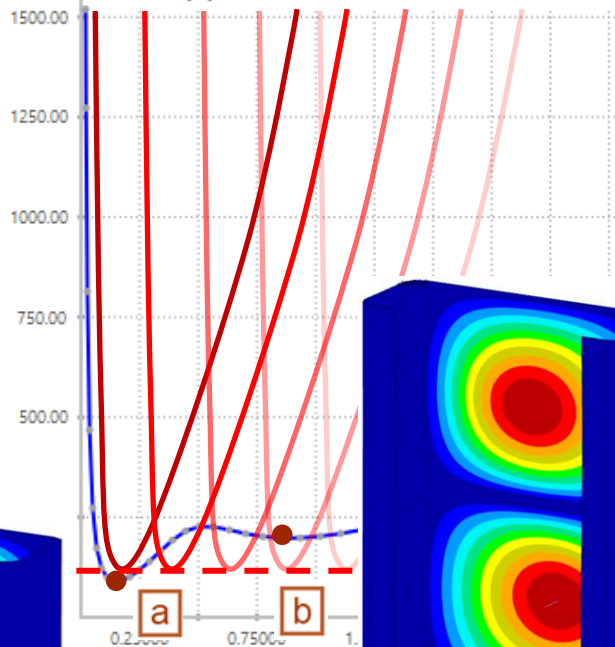
**Warping torsion** required to account for those modes in static / stability analysis!



- Structural element is divided into multiple strips (strip length = system length)
- Advantage: Cross section deformation can be investigated (as opposed to beam elements) with very few DOFs (compared to a accurate shell representation)
- Boundary conditions for stability analysis: simply supported (including fork conditions)
- Due to the discretization in longitudinal direction (1 strip/simple shape function) only bow shaped deformations are considered

$\delta_{ki}$  | N: -1 kN | Buckling shape | FSM | L: 0.85261 m |  $\delta_{ki}$ : 197.77

Critical load factor  $\delta_{ki}$   
[--]

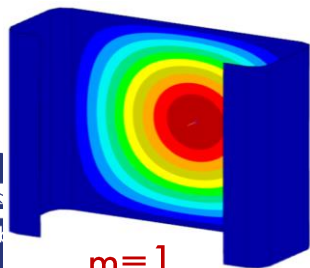


a

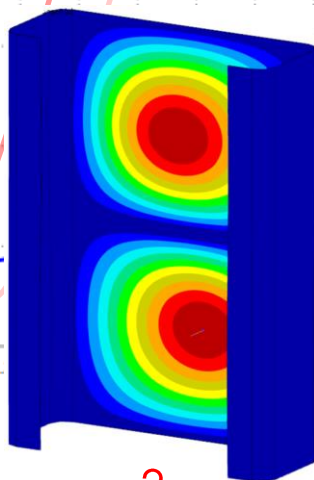
b

c

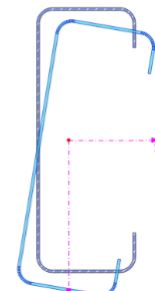
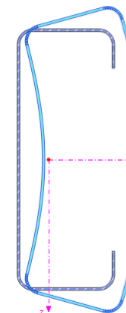
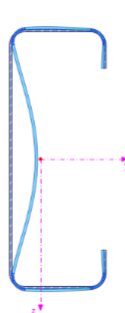
Length  $L$   
[m]



$m=1$



$m=2$





## Additional Information

- [1] Knowledge Base 1851: Modal Relevance Factor  
<https://www.dlubal.com/en/support-and-learning/support/knowledge-base/001851>
- [2] Knowledge Base 1801 : Linear Critical Load Analysis Using Finite Strip Method (FSM)  
<https://www.dlubal.com/en/support-and-learning/support/knowledge-base/001801>
- [3] FAQ 005345: My model is unstable. What could be the reason?  
<https://www.dlubal.com/en/support-and-learning/support/faq/005345>

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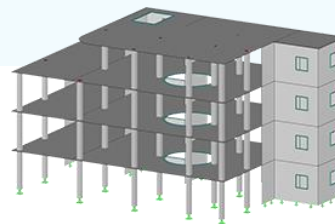
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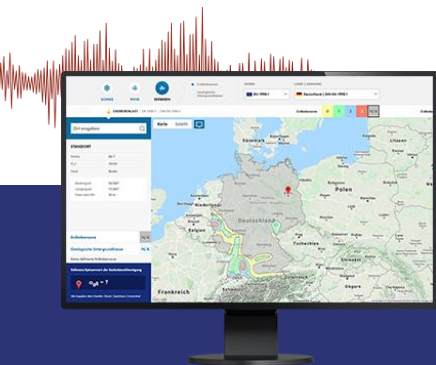


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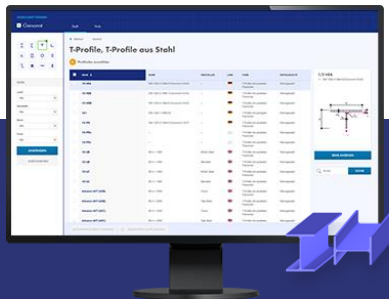
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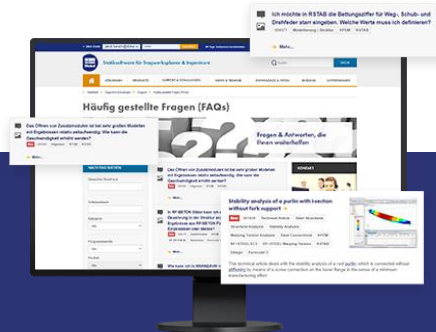
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With this free online tool, you can select standardized sections from an extensive section library, define parametrized cross-sections and calculate its cross-section properties.



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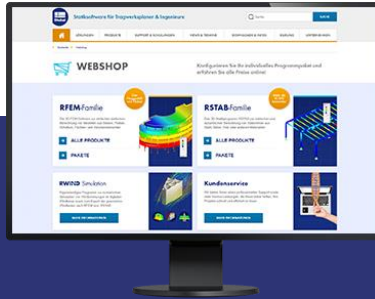
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Videos and webinars about the structural engineering software.



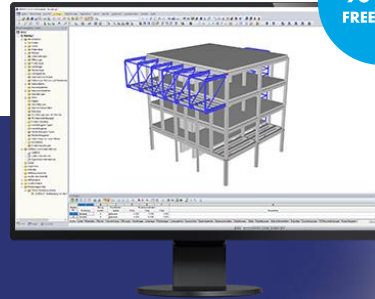
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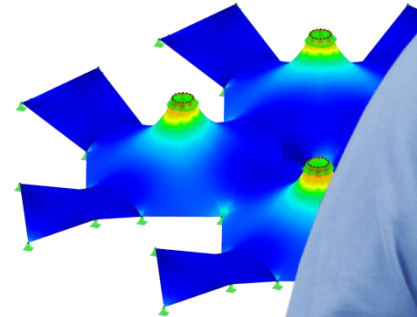
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